



Full length article

Secrecy rate maximization in multi-IRS mmWave networks

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ARTICLE INFO

Article history:

Received 12 February 2021

Received in revised form 2 July 2021

Accepted 21 July 2021

Available online 30 July 2021

Keywords:

Intelligent Reflecting Surface (IRS)

Multiple IRSs

MmWave communications

Physical layer security

ABSTRACT

This paper investigates the problem of improving security at the physical layer of a Millimeter Wave (mmWave) network equipped with multiple Intelligent Reflecting Surfaces (IRSs). In this network, the IRSs help the Base Station (BS) in transmitting its signal to the desired user and at the same time improving the physical layer security of the network by preventing the signal to be received by an illegitimate eavesdropper. The target of the proposed scheme is to maximize the secrecy rate by jointly optimizing the active beamforming at the BS and passive beamforming at the IRSs. This is done through a non-convex optimization problem which is solved by decomposing into two sub-problems. The sub-problems are alternatively solved using the Semi-Definite Relaxation (SDR) technique. Finally, simulations are done to assess the performance of the proposed algorithm. These results show the superiority of using multiple IRSs in the enhancement of secrecy rate of the wireless networks in the mmWave frequency bands.

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1. Introduction

One of the key technologies in current and future generations of wireless networks is millimeter Wave (mmWave) communications [1]. The main advantages of the mmWave frequency bands are higher bandwidth, higher frequency reuse, less interference, and smaller antenna array dimensions. Despite these benefits, mmWave communications are more sensitive to blockage and suffer from a large attenuation compared with lower frequencies [1]. On the other hand, Intelligent Reflecting Surface (IRS) or Reconfigurable Intelligent Surface (RIS) is a novel technology that has been recently proposed to improve the performance of wireless communication networks. [2]. These are metasurfaces that can control the propagation direction of the wireless signals to focus them on a point of interest and improve the wireless link qualities [3]. The IRSs can also be employed in the mmWave networks to compensate for the blockage effect and high path loss in these networks.

1.1. Related work

Passive beamforming design for the IRSs in the microwave bands was extensively studied in literature [4,5]. Wang et al. in [5] proposed an algorithm to maximize users' received power by joint active and passive beamforming in multi-IRSs assisted communications. In [6], it was shown that an increase in the number

of reflecting elements of an IRS leads to the BS's power can be decreased quadratically. Also in [7], an optimized beamforming and power allocation method was proposed for maximizing the total rate in the mmWave systems where multi-IRSs are employed. In [8], the authors focused on minimizing BS's transmitted power and jointly optimizing active and passive beamforming.

Due to the passive nature and a high number of reflecting elements in IRSs, channel estimation in the IRS-assisted systems becomes a challenging issue that has been investigated in some recent literature [9–11]. In most of these papers, channels are partially estimated and extrapolated using the deep learning approach. In [9], the authors considered an IRS that is equipped with some active elements and can acquire their partially Channel State Information (CSI). The locations of these active elements were derived based on probabilistic sampling theory. Two deep learning-based schemes, namely, channel extrapolation and beam searching were also designed. The authors in [10] proposed an Ordinary Differential Equation based Convolutional Neural Network (ODE-CNN) approach to acquire full CSI from extrapolation of the partial CSI. But in contrast to [9], they only used passive elements and turned on a fractional part of IRSs' elements. They also showed that their proposed method can have a faster convergence rate and achieve a better solution than cascaded CNN. In [11], to reduce IRS channel training overhead in a system consisting of a large number of BS antennas or IRS reflecting elements, three types of channel extrapolation namely, antenna, frequency, and physical terminal extrapolations were proposed.

The problem of physical layer security in IRS-aided networks has been also studied in recent literature. For example, joint

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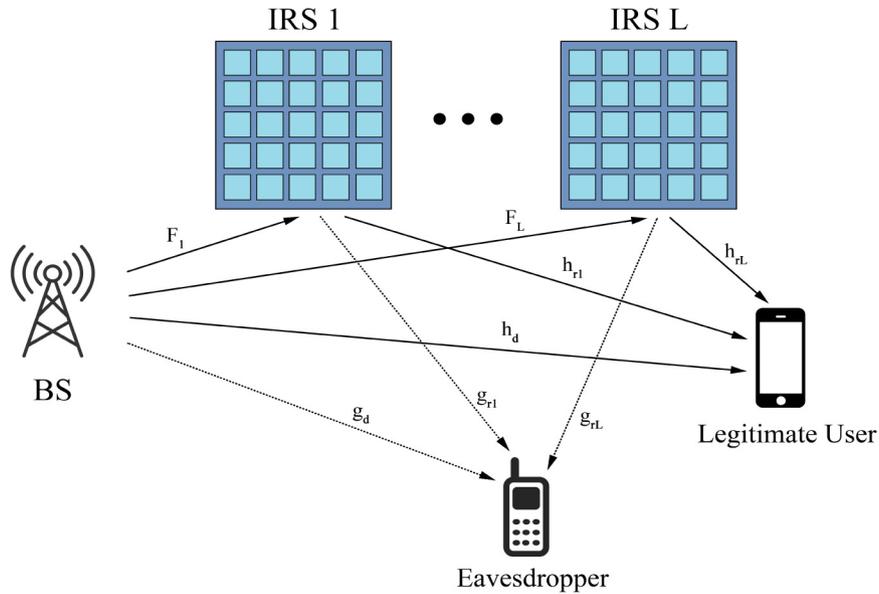


Fig. 1. A multi IRS-aided mmWave communication network consisting a single legitimate user and an eavesdropper.

optimizing of the BS beamforming and IRS phase shifts for secrecy rate maximization was considered in [12–14]. Furthermore, using artificial noise for enhancing the secrecy rate of an IRS network was studied in [15]. By employing a physical layer security approach, the authors in [16] have jointly designed beamforming matrix and artificial noise signals at the base station, and the phase shifts of the IRS's to improve the sum rate of a multi-IRS system. An IRS-assisted mmWave network was studied in [17] in which the network secrecy rate was enhanced by applying an alternating optimization-based method and joint optimization of the IRS phase shift and the beamforming at the transmitter. To do this end, the authors employed two approaches namely, element-wise block coordinate descent and successive convex approximation (SCA). The combination of physical layer security and channel estimation in an IRS-assisted system was also investigated [18,19]. The authors in [18] investigated secure beamforming by employing a deep reinforcement learning approach under the time-varying channel assumption. To improve the learning efficiency, they used a post-decision state and prioritized experience replay. Their results showed a considerable improvement in secrecy rate and QoS satisfaction probability compared with traditional methods. Yang et al. considered an IRS-aided anti-jamming system, where IRS can mitigate the jamming interference by joint power allocation at the BS and phase shift design at the IRS using the fuzzy win or learn fast-policy hill-climbing approach. Simulation results demonstrated the IRS-aided system enhances the system rate and transmission protection level compared with existing approaches [19].

However, the problem of multi-IRS networks operating in the mmWave frequency bands is still an open problem and on the other hand, the problem of secrecy rate maximization in multi-IRS mmWave has not been widely studied in the literature.

1.2. Contribution

In this paper, motivated by the following facts, we study the problem of physical layer security in a multi-IRS aided millimeter-wave network. In this mmWave network, the IRSs are utilized to create multiple links between a multiple-antenna BS and a user, and at the same time, an eavesdropper listens to these signals. Both the user and eavesdropper utilize a single antenna for signal transmission and reception. The target of the proposed method

is maximizing the network secrecy rate by jointly optimizing the beamforming coefficients at the base station and phase shifts at the IRSs. This results in a non-convex optimization problem and to solve it we design an efficient method that is based on alternating method and Semi-Definite Relaxation (SDR) technique. Finally, we present simulation results to show the advantages of using multiple IRSs in the mmWave network for secrecy rate enhancement.

Our main contributions can be summarized as follows:

- In most papers, a single IRS in a wireless network is considered, But we study a network equipped with multiple IRS. By increasing the number of IRSs in the mmWave band, the extra paths from the BS to the user are created, which improves the received power in the user and thus increases the secrecy rate. Due to the high path loss and blockage sensitivity in the mmWave frequency bands, it is more necessary to create more paths in this band compared to the microwave band.
- In most papers, to increase the impact of IRSs on system performance, direct link between the BS and the intended receivers is ignored. But, since both the base station and reflecting surfaces are usually located at high altitudes, the probability that both of them have direct links is high. Thus, in this paper, we suggest a more practical setup in which direct channels between BS and user and also BS and eavesdropper are also considered to exist.
- We propose a new solution method for the beamforming and IRS phases optimization in the multi-IRSs networks. In this method, we divide our non-convex optimization problem into two sub-problems. After that, by definition of proper variables, Semi-Definite Relaxation (SDR) and Charnes–Cooper Transformation (CCT), we propose an algorithm to achieve a sub-optimal solution. Then, we evaluate the complexity and convergence of this algorithm.

The rest of the paper is organized as follows. In Section 2, the system and channel model, as well as problem formulation, are introduced. In Section 3, the proposed algorithm for solving the optimization problem is proposed and in Section 4, we present simulation results. Finally, Section 5 demonstrates the paper's conclusions.

2. System model, channel model and problem formulation

2.1. System model

As shown in Fig. 1, we consider the downlink of a mmWave network where a BS serves a user in the presence of an eavesdropper. The BS is equipped with M antennas and the user and eavesdropper each has one antenna. Also, each L IRS has N reflecting elements that assist in secure communication from the BS to the user. The reflecting elements of the IRSs change the phase of the received signal and then forward it towards the user. Although, our main focus is on the single-user network, it can be further extended to a multi-user scenario. It should be noted that this single-user model can be applied to practical wireless systems in which the users are separated in time or frequency domains and at each resource block (assigned a single user) an eavesdropper tries to secretly listen to the data.

The channel coefficients $\mathbf{F}_l \in \mathbb{C}^{N \times M}$, $\mathbf{h}_d \in \mathbb{C}^{M \times 1}$, $\mathbf{g}_d \in \mathbb{C}^{M \times 1}$, $\mathbf{h}_{rl} \in \mathbb{C}^{N \times 1}$, and $\mathbf{g}_{rl} \in \mathbb{C}^{N \times 1}$ are addressed the channel between the bases station and the l th IRS, the bases station and the user, the bases station and the eavesdropper, the l th IRS and the user, and the l th IRS and eavesdropper, respectively. We consider the perfectly estimated CSI at the BS. The transmitted signal from the base station is denoted by s that is with zero mean and unit variance. The beamforming vector at the BS is represented by \mathbf{w} that satisfies $\|\mathbf{w}\|^2 \leq P_{BS}$, where P_{BS} is the maximum allowable transmit power of the bases station.

The received signal at the legitimate user can be written as

$$y_r = \left(\sum_{l=1}^L \mathbf{h}_{rl}^H \Theta_l \mathbf{F}_l + \mathbf{h}_d^H \right) \mathbf{w} s + n_r, \quad (1)$$

where n_r with zero mean and variance σ_r^2 is Additive White Gaussian Noise (AWGN) at the user.

$\Theta_l = \text{diag}\{e^{j\theta_{l,1}}, e^{j\theta_{l,2}}, \dots, e^{j\theta_{l,N}}\} = \text{diag}\{\alpha_{l,1}, \alpha_{l,2}, \dots, \alpha_{l,N}\} = \text{diag}\{\alpha_l\}$ is a diagonal matrix that denotes the effective phase shifts at the IRS elements and $\theta_{l,n} \in [0, 2\pi)$ is the phase shift of the n th reflecting element of the l th IRS. Similar to (1), the received signal at the eavesdropper is also obtained as

$$y_e = \left(\sum_{l=1}^L \mathbf{g}_{rl}^H \Theta_l \mathbf{F}_l + \mathbf{g}_d^H \right) \mathbf{w} s + n_e, \quad (2)$$

where n_e is additive white Gaussian noise at the eavesdropper which has zero mean and its variance is σ_e^2 . In the system model that we consider in this paper, the effect of signal reflection between the IRSs is not considered. The reason is that this system is in the mmWave frequency bands and the path loss is very severe in these frequencies. Hence, multiple reflections by the IRS can be easily ignored.

Using (1) and (2), the achievable rates of the user and the eavesdropper are given by

$$R_r = \log_2 \left(1 + \frac{\left| \left(\sum_{l=1}^L \mathbf{h}_{rl}^H \Theta_l \mathbf{F}_l + \mathbf{h}_d^H \right) \mathbf{w} \right|^2}{\sigma_r^2} \right), \quad (3)$$

and

$$R_e = \log_2 \left(1 + \frac{\left| \left(\sum_{l=1}^L \mathbf{g}_{rl}^H \Theta_l \mathbf{F}_l + \mathbf{g}_d^H \right) \mathbf{w} \right|^2}{\sigma_e^2} \right), \quad (4)$$

respectively. Then, the secrecy rate is obtained by $R_s = [R_r - R_e]^+$, where $[z]^+ = \max(z, 0)$. Thus, the secrecy rate can be obtained as

$$R_s = \left[\log_2 \left(1 + \frac{\left| \left(\sum_{l=1}^L \mathbf{h}_{rl}^H \Theta_l \mathbf{F}_l + \mathbf{h}_d^H \right) \mathbf{w} \right|^2}{\sigma_r^2} \right) \right]^+ - \left[\log_2 \left(1 + \frac{\left| \left(\sum_{l=1}^L \mathbf{g}_{rl}^H \Theta_l \mathbf{F}_l + \mathbf{g}_d^H \right) \mathbf{w} \right|^2}{\sigma_e^2} \right) \right]^+.$$

$$- \log_2 \left(1 + \frac{\left| \left(\sum_{l=1}^L \mathbf{g}_{rl}^H \Theta_l \mathbf{F}_l + \mathbf{g}_d^H \right) \mathbf{w} \right|^2}{\sigma_e^2} \right) \right]^+. \quad (5)$$

2.2. MmWave channel model

The BS-to-user channel \mathbf{h}_d is modeled using a geometric channel model of the mmWave communications [20] which can be expressed as

$$\mathbf{h}_d = \frac{\sqrt{M}}{K} \sum_{k=1}^K \rho_{k,b}^u G_b \mathbf{a}_b(\phi_{k,b}^u), \quad (6)$$

where K is total number of paths, $\rho_{k,b}^u \sim \mathcal{CN}(0, 10^{-0.1PL(d)})$ is the complex gain of the k th path between BS and user, G_b is the BS antenna gain. $\mathbf{a}_b(\phi_{k,b}^u)$ is the normalized BS array response vector at an azimuth Angle of Departure AoD $\phi_{k,b}^u \in [0, 2\pi]$. The path loss can be obtained as [21]

$$PL(d) [\text{dB}] = \mu + 10\kappa \log_{10}(d) + \xi, \quad (7)$$

in which d , μ and κ denote the distance between transmitter and receiver, constant path loss term and path loss exponent, respectively. Also $\xi \sim N(0, \sigma_\xi^2)$ where σ_ξ^2 is shadowing variance.

Similar to (6), the BS-to-eavesdropper channel can be modeled by

$$\mathbf{g}_d = \frac{\sqrt{M}}{K} \sum_{k=1}^K \rho_{k,b}^e G_b \mathbf{a}_b(\phi_{k,b}^e), \quad (8)$$

where $\rho_{k,b}^e \sim \mathcal{CN}(0, 10^{-0.1PL(d)})$ is the complex gain of the k th path between BS and eavesdropper. $\mathbf{a}_b(\phi_{k,b}^e)$ is the normalized BS array response vector at an azimuth AoD $\phi_{k,b}^e \in [0, 2\pi]$.

With the assumption that the BS and IRSs are located at a higher altitude, the channels between them are assumed to be LOS dominant. Thus the BS-to- l th IRS channel can be modeled as a rank-one matrix [7]

$$\mathbf{F}_l = \sqrt{MN} \rho_b^l G_b \mathbf{a}_l(\phi_l^b, \psi_l^b) \mathbf{a}_b^H(\phi_b^l), \quad l \in \{1, 2, \dots, L\}, \quad (9)$$

where $\rho_b^l \sim \mathcal{CN}(0, 10^{-0.1PL(d)})$ denotes the complex gain of the BS-to- l th IRS channel that $PL(d)$ is derived according to (7). $\phi_l^b \in [0, \pi]$ is the elevation and azimuth Angles of Arrival (AoA) for the l th IRS and $\phi_b^l \in [0, 2\pi]$ is the azimuth AoD for the BS. $\mathbf{a}_l(\phi_l^b, \psi_l^b)$ is the normalized l th IRS array response vector, that is denoted by

$$\mathbf{a}_l(\phi_l^b, \psi_l^b) = \mathbf{a}_l^{az}(\psi_l^b) \otimes \mathbf{a}_l^{el}(\phi_l^b), \quad (10)$$

where $\mathbf{a}_l^{az}(\psi_l^b)$ and $\mathbf{a}_l^{el}(\phi_l^b)$ are the horizontal and vertical array response vector of the l th IRS, respectively. Also $\mathbf{a}_b(\phi_b^l)$ is the normalized BS array response vector.

Similar to (6) and (8), the l th IRS to user and eavesdropper channels can be respectively given by

$$\mathbf{h}_{rl} = \frac{\sqrt{N}}{K} \sum_{k=1}^K \rho_{k,l}^u G_l \mathbf{a}_l(\phi_{k,l}^u, \psi_{k,l}^u), \quad (11)$$

and

$$\mathbf{g}_{rl} = \frac{\sqrt{N}}{K} \sum_{k=1}^K \rho_{k,l}^e G_l \mathbf{a}_l(\phi_{k,l}^e, \psi_{k,l}^e), \quad (12)$$

where $\rho_{k,l}^u \sim \mathcal{CN}(0, 10^{-0.1PL(d)})$ and $\rho_{k,l}^e \sim \mathcal{CN}(0, 10^{-0.1PL(d)})$ are the complex gain of the k th path of l th IRS-user channel and l th IRS-eavesdropper channel, respectively. $\phi_{k,l}^u \in [0, \pi]$ and $\psi_{k,l}^u \in [0, \pi]$ are the azimuth and elevation (AoD) for the l th IRS, respectively. Also $\phi_{k,l}^e \in [0, \pi]$ and $\psi_{k,l}^e \in [0, \pi]$ are the azimuth and elevation AoD for the l th IRS. $\mathbf{a}_l(\phi_{k,l}^u, \psi_{k,l}^u)$ and $\mathbf{a}_l(\phi_{k,l}^e, \psi_{k,l}^e)$ are

the normalized array response vectors of the l th IRS associated with the IRS-user and the IRS-eavesdropper paths, respectively. Definition of $\mathbf{a}_l(\phi_{k,l}^u, \psi_{k,l}^u)$ and $\mathbf{a}_l(\phi_{k,l}^e, \psi_{k,l}^e)$ are similar to (10) based on Kronecker product of the l th IRS horizontal and vertical array response vectors.

2.3. Problem formulation

Based on the aforementioned discussion, this paper focuses on maximizing the secrecy rate by jointly optimizing the transmit beamforming vector \mathbf{w} at the BS and the phase vectors $\{\alpha_1, \dots, \alpha_L\}$ at the IRSs, under the BS's maximum transmission power and unit modulus of the diagonal elements of $\{\Theta_1, \dots, \Theta_L\}$ constraints. This problem can be expressed as

$$P: \max_{\mathbf{w}, \alpha_1, \alpha_2, \dots, \alpha_L} R_s \quad (13a)$$

$$\text{s.t. } \|\mathbf{w}\|^2 \leq P_{BS} \quad (13b)$$

$$|\alpha_{l,n}| = 1, \quad l \in \{1, \dots, L\}, \quad n \in \{1, \dots, N\}. \quad (13c)$$

Because of the coupled variables \mathbf{w} and $\{\alpha_1, \dots, \alpha_L\}$ in the objective and constraint functions, this problem (P) is a non-convex problem.

3. Proposed algorithm and beamforming design

By decomposing the optimization variables in (13) into two individual subsets of \mathbf{w} and $\{\alpha_1, \dots, \alpha_L\}$, it is found that (13b) and (13c) represents two disjoint sets on \mathbf{w} and $\{\alpha_1, \dots, \alpha_L\}$, respectively. Thus, the problem can be solved alternatively by maximization of \mathbf{w} and $\{\alpha_1, \dots, \alpha_L\}$ in an iterative manner through two disjoint sub-problems. At each iteration, first for a given value of $\{\alpha_1, \dots, \alpha_L\}$, a solution for optimized \mathbf{w} is derived. Then, the second sub-problem is solved for the optimized \mathbf{w} and this procedure is iterated until convergence. Both sub-problems are solved using the SDR technique and CCT. To extend the following proposed solution algorithm to the multi-user case, the most challenging part is to handle the interference among users. However, there are some ideas to overcome this challenge such as the transformation of objective to constraints and using successive convex approximation method [22].

3.1. Sub-problem 1

First, we assume that the parameters $\{\alpha_1, \dots, \alpha_L\}$ are fixed and derive the optimal value of \mathbf{w} . To this end, the objective function in problem (P) is reformulated, and then considering that the log function is monotonically increasing, it is removed. Therefore, sub-problem 1 will be

$$\max_{\mathbf{w}} \left(\frac{1 + \frac{1}{\sigma_r^2} \left| \left(\sum_{l=1}^L \mathbf{h}_{rl}^H \Theta_l \mathbf{F}_l + \mathbf{h}_d^H \right) \mathbf{w} \right|^2}{1 + \frac{1}{\sigma_e^2} \left| \left(\sum_{l=1}^L \mathbf{g}_{rl}^H \Theta_l \mathbf{F}_l + \mathbf{g}_d^H \right) \mathbf{w} \right|^2} \right) \quad (14a)$$

$$\text{s.t. } \|\mathbf{w}\|^2 \leq P_{BS}. \quad (14b)$$

By defining $\mathbf{h}_{user} = \left(\sum_{l=1}^L \mathbf{h}_{rl}^H \Theta_l \mathbf{F}_l + \mathbf{h}_d^H \right) \in \mathbb{C}^{1 \times M}$, $\mathbf{g}_{eve} = \left(\sum_{l=1}^L \mathbf{g}_{rl}^H \Theta_l \mathbf{F}_l + \mathbf{g}_d^H \right) \in \mathbb{C}^{1 \times M}$ and $\mathbf{W} = \mathbf{w}\mathbf{w}^H \in \mathbb{C}^{M \times M}$, we have

$$\left| \left(\sum_{l=1}^L \mathbf{h}_{rl}^H \Theta_l \mathbf{F}_l + \mathbf{h}_d^H \right) \mathbf{w} \right|^2 = \mathbf{h}_{user} \mathbf{W} \mathbf{h}_{user}^H \quad (15)$$

and

$$\left| \left(\sum_{l=1}^L \mathbf{g}_{rl}^H \Theta_l \mathbf{F}_l + \mathbf{g}_d^H \right) \mathbf{w} \right|^2 = \mathbf{g}_{eve} \mathbf{W} \mathbf{g}_{eve}^H. \quad (16)$$

We can rewrite (14) into a linear fractional problem as

$$P.1: \max_{\mathbf{w}} \left(\frac{1 + \frac{1}{\sigma_r^2} \mathbf{h}_{user} \mathbf{W} \mathbf{h}_{user}^H}{1 + \frac{1}{\sigma_e^2} \mathbf{g}_{eve} \mathbf{W} \mathbf{g}_{eve}^H} \right) \quad (17a)$$

$$\text{s.t. } \text{Tr}(\mathbf{W}) \leq P_{BS} \quad (17b)$$

$$\mathbf{W} \succeq 0 \quad (17c)$$

$$\text{Rank}(\mathbf{W}) = 1. \quad (17d)$$

In this problem, we first use SDR to relax the rank-one constraint (17d). Then by employing the CCT method, \mathbf{W} is obtained, and finally, to satisfy the (17d), a rank one approximation of \mathbf{W} is derived using the Gaussian randomization method.

By dropping (17d), using the CCT and defining $\gamma = \frac{1}{1 + \frac{1}{\sigma_e^2} (\mathbf{g}_{eve} \mathbf{W} \mathbf{g}_{eve}^H)}$ and $\mathbf{T} = \gamma \mathbf{W}$, (17) is transformed into the following

non-fractional problem

$$\max_{\mathbf{T}, \gamma} \gamma + \frac{1}{\sigma_r^2} (\mathbf{h}_{user} \mathbf{T} \mathbf{h}_{user}^H) \quad (18a)$$

$$\text{s.t. } \gamma + \frac{1}{\sigma_e^2} (\mathbf{g}_{eve} \mathbf{T} \mathbf{g}_{eve}^H) = 1 \quad (18b)$$

$$\text{Tr}(\mathbf{T}) \leq \gamma P_{BS} \quad (18c)$$

$$\mathbf{T} \succeq 0, \gamma \geq 0. \quad (18d)$$

The problem in (18) is a Semi-Definite Programming (SDP) problem and therefore it is convex and CVX can be used to solve such a problem. After solving (18), \mathbf{W} is obtained as \mathbf{T}/γ . Then, to satisfy the constraint $\text{Rank}(\mathbf{W}) = 1$, according to [23] we use the standard Gaussian randomization method to achieve an approximation for \mathbf{w} .

3.2. Sub-problem 2

In the next step, for a given \mathbf{w} , the problem (P) is transformed to sub-problem 2 that can be formulated as follows [14]

$$\max_{\alpha_1, \alpha_2, \dots, \alpha_L} \frac{\left(1 + \frac{1}{\sigma_r^2} \left| \left(\sum_{l=1}^L \mathbf{h}_{rl}^H \Theta_l \mathbf{F}_l + \mathbf{h}_d^H \right) \mathbf{w} \right|^2 \right)}{\left(1 + \frac{1}{\sigma_e^2} \left| \left(\sum_{l=1}^L \mathbf{g}_{rl}^H \Theta_l \mathbf{F}_l + \mathbf{g}_d^H \right) \mathbf{w} \right|^2 \right)} \quad (19)$$

$$\text{s.t. } |\alpha_{l,n}| = 1, \quad l \in \{1, 2, \dots, L\}, \quad n \in \{1, 2, \dots, N\}.$$

Then, using the equality $\mathbf{c} \Theta_l = \alpha_l^T \text{diag}(\mathbf{c})$, where Θ_l is the l th IRS phase shift matrix and α_l is the phase vector of the l th IRS, and also defining $\mathbf{c} = \mathbf{h}_{rl}^H$ and $\mathbf{c} = \mathbf{g}_{rl}^H$, we can write

$$\sum_{l=1}^L \left(\mathbf{h}_{rl}^H \Theta_l \mathbf{F}_l + \frac{1}{L} \mathbf{h}_d^H \right) \mathbf{w} = \sum_{l=1}^L \left(\alpha_l^T \text{diag}(\mathbf{h}_{rl}^H) \mathbf{F}_l + \frac{1}{L} \mathbf{h}_d^H \right) \mathbf{w} \quad (20)$$

$$\sum_{l=1}^L \left(\mathbf{g}_{rl}^H \Theta_l \mathbf{F}_l + \frac{1}{L} \mathbf{g}_d^H \right) \mathbf{w} = \sum_{l=1}^L \left(\alpha_l^T \text{diag}(\mathbf{g}_{rl}^H) \mathbf{F}_l + \frac{1}{L} \mathbf{g}_d^H \right) \mathbf{w}. \quad (21)$$

Then, (20) and (21) can be further simplified as follows

$$\sum_{l=1}^L \left(\mathbf{h}_{rl}^H \Theta_l \mathbf{F}_l + \frac{1}{L} \mathbf{h}_d^H \right) \mathbf{w} = \mathbf{x}_l^H \mathbf{h}'_{user,l} \quad (22)$$

$$\sum_{l=1}^L \left(\mathbf{g}_{rl}^H \Theta_l \mathbf{F}_l + \frac{1}{L} \mathbf{g}_d^H \right) \mathbf{w} = \mathbf{x}_l^H \mathbf{g}'_{eve,l} \quad (23)$$

where $\mathbf{x}_l = [\alpha_l^T, \frac{1}{L}]^H \in \mathbb{C}^{(N+1) \times 1}$, and

$$\mathbf{h}'_{user,l} = \begin{pmatrix} \text{diag}(\mathbf{h}_{rl}^H) \mathbf{F}_l \mathbf{w} \\ \mathbf{h}_d^H \mathbf{w} \end{pmatrix} \in \mathbb{C}^{(N+1) \times 1} \quad (24a)$$

$$\mathbf{g}'_{eve,l} = \begin{pmatrix} \text{diag}(\mathbf{g}'_l^H) \mathbf{F}_l \mathbf{w} \\ \mathbf{g}'_l^H \mathbf{w} \end{pmatrix} \in \mathbb{C}^{(N+1) \times 1}. \quad (24b)$$

By substitution of (22) and (23) for objective function of (19), sub-problem 2 can be reformulated as

$$\max_{\mathbf{x}_1, \mathbf{x}_2, \dots, \mathbf{x}_L} \frac{(1 + \frac{1}{\sigma_r^2} \sum_{l=1}^L |\mathbf{x}_l^H \mathbf{h}'_{user,l}|^2)}{(1 + \frac{1}{\sigma_e^2} \sum_{l=1}^L |\mathbf{x}_l^H \mathbf{g}'_{eve,l}|^2)} \quad (25a)$$

$$\text{s.t. } \mathbf{x}_l^H \mathbf{S}_l \mathbf{x}_l = 1, \forall l, \quad (25b)$$

where \mathbf{S}_l is defined to satisfy the unit modules constraint of the IRS element gain and its (k, j) th element is denoted by

$$[\mathbf{S}_l]_{k,j} = \begin{cases} 1 & i = k = j, i \in \{1, \dots, L-1\} \\ L^2 & i = k = j = L \\ 0 & \text{otherwise} \end{cases} \quad (26)$$

The objective function (25a) is a quadratically fractional function and the constraint (25b) is quadratic equality and non-convex and hence, the problem (25) is not a convex problem.

By defining $\mathbf{X}_l = \mathbf{x}_l \mathbf{x}_l^H$, the numerator of (25a) is expressed as

$$1 + \frac{1}{\sigma_r^2} \sum_{l=1}^L |\mathbf{x}_l^H \mathbf{h}'_{user,l}|^2 = 1 + \frac{1}{\sigma_r^2} \sum_{l=1}^L \mathbf{h}'_{user,l}{}^H \mathbf{x}_l \mathbf{x}_l^H \mathbf{h}'_{user,l} = 1 + \frac{1}{\sigma_r^2} \sum_{l=1}^L \mathbf{h}'_{user,l}{}^H \mathbf{X}_l \mathbf{h}'_{user,l} \quad (27)$$

and denominator of (25b) is expressed as

$$1 + \frac{1}{\sigma_e^2} \sum_{l=1}^L |\mathbf{x}_l^H \mathbf{g}'_{eve,l}|^2 = 1 + \frac{1}{\sigma_e^2} \sum_{l=1}^L \mathbf{g}'_{eve,l}{}^H \mathbf{x}_l \mathbf{x}_l^H \mathbf{g}'_{eve,l} = 1 + \frac{1}{\sigma_e^2} \sum_{l=1}^L \mathbf{g}'_{eve,l}{}^H \mathbf{X}_l \mathbf{g}'_{eve,l} \quad (28)$$

According to (28) and (29), we rewrite (25) into a linear fractional problem as

$$\max_{\mathbf{x}_1, \dots, \mathbf{x}_L} \frac{1 + \frac{1}{\sigma_r^2} \sum_{l=1}^L (\mathbf{h}'_{user,l}{}^H \mathbf{X}_l \mathbf{h}'_{user,l})}{1 + \frac{1}{\sigma_e^2} \sum_{l=1}^L (\mathbf{g}'_{eve,l}{}^H \mathbf{X}_l \mathbf{g}'_{eve,l})} \quad (29a)$$

$$\text{s.t. } \text{tr}(\mathbf{S}_l \mathbf{X}_l) = 1, \forall l, \quad (29b)$$

$$\text{Rank}(\mathbf{X}_l) = 1, \forall l, \quad (29c)$$

$$\mathbf{X}_l \geq 0. \quad (29d)$$

Similar to the first sub-problem, we drop rank one constraint, then use CCT to obtain $\mathbf{X}_l, \forall l$ and finally by employing the Gaussian randomization method, we find an approximated rank-one solution.

In the following, by dropping (27)c, using the CCT and defining $\lambda = 1/(1 + \frac{1}{\sigma_e^2} \sum_{l=1}^L (\mathbf{g}'_{eve,l}{}^H \mathbf{X}_l \mathbf{g}'_{eve,l}))$ and $\mathbf{T}_l = \lambda \mathbf{X}_l$, (30) is transformed into the following non-fractional problem

$$P.2 : \max_{\mathbf{T}_1, \dots, \mathbf{T}_L, \lambda} \lambda + \frac{1}{\sigma_r^2} \sum_{l=1}^L (\mathbf{h}'_{user,l}{}^H \mathbf{T}_l \mathbf{h}'_{user,l}) \quad (30a)$$

$$\text{s.t. } \lambda + \frac{1}{\sigma_e^2} \sum_{l=1}^L (\mathbf{g}'_{eve,l}{}^H \mathbf{T}_l \mathbf{g}'_{eve,l}) = 1 \quad (30b)$$

$$\text{tr}(\mathbf{S}_l \mathbf{T}_l) = \lambda, \forall l, \quad (30c)$$

$$\mathbf{T}_l \geq 0, \forall l \quad (30d)$$

$$\lambda \geq 0 \quad (30e)$$

The problem in (31) is an SDP problem and therefore a convex optimization problem. After solving (31), \mathbf{X}_l is obtained as \mathbf{T}_l/λ .

Similar to \mathbf{w} , an approximate solution to \mathbf{x}_l can be obtained by standard Gaussian randomization.

Our final proposed algorithm to find the solution of problem P is presented in **Algorithm 1**.

Algorithm 1 Proposed alternating iterative algorithm for solving P.

Outputs: $\mathbf{w}, \Theta_1, \Theta_2, \dots, \Theta_L, R_s$.

Initialization: $i = 0, \mathbf{w}^{(0)}, \Theta_1^{(0)} = \Theta_2^{(0)} = \dots = \Theta_L^{(0)}, \varepsilon = 10^{-3}$.

1: **Repeat**

2: Set $i = i + 1$.

3: Using $\Theta_1^{(i-1)}, \Theta_2^{(i-1)}, \dots, \Theta_L^{(i-1)}$, Solve P.1 and obtain $\mathbf{T}^{(i)}$ and $\lambda^{(i)}$.

4: Set $\mathbf{W}^{(i)} = \mathbf{T}^{(i)}/\lambda^{(i)}$ and derive $\mathbf{w}^{(i)}$ by employing the Gaussian Randomization method.

5: With given $\mathbf{w}^{(i)}$, Solve the P.2 and find $\mathbf{T}_1^{(i)}, \mathbf{T}_2^{(i)}, \dots, \mathbf{T}_L^{(i)}$ and $\lambda^{(i)}$.

6: Set $\mathbf{X}_l^{(i)} = \mathbf{T}_l^{(i)}/\lambda^{(i)}; \forall l \in \{1, 2, \dots, L\}$ and derive $\Theta_1^{(i)}, \Theta_2^{(i)}, \dots, \Theta_L^{(i)}$ by employing the Gaussian Randomization method.

7: **Until** $\left| \frac{R_s^{(i)} - R_s^{(i-1)}}{R_s^{(i-1)}} \right| \leq \varepsilon$.

3.3. Convergence of the proposed algorithm

In the following theorem, we discuss the convergence behavior of our proposed algorithm.

Theorem 1. *Our proposed algorithm converges to a finite value in a non-decreasing fashion.*

Proof. Based on the following equation we find that the objective function has a non-decreasing behavior at the successive iterations.

$$R_s(\mathbf{W}^{(i-1)}, \Theta_0^{(i-1)}, \dots, \Theta_L^{(i-1)}) \leq R_s(\mathbf{W}^{(i)}, \Theta_0^{(i-1)}, \dots, \Theta_L^{(i-1)}) \leq R_s(\mathbf{W}^{(i)}, \Theta_0^{(i)}, \dots, \Theta_L^{(i)}) \quad (31)$$

The first inequality follows the fact that at the i th iteration in the first sub-problem, for the given Θ which is derived from the last iteration, \mathbf{W} is optimized, thus the objective function improves. In the second inequality, this process is repeated for the given \mathbf{W} and the objective function grows by optimizing Θ . Due to the limited resource such as power, the number of antennas, and IRSs, the final value of the secrecy rate is upper bounded and the algorithm converges to a finite value in a non-decreasing fashion. \square

3.4. Complexity of the proposed algorithm

Algorithm 1 requires solving two convex problems (18) and (30), at each iteration. The complexity of steps (3) and (4), which is related to the convex problem (18), is $\mathcal{O}(M^{3.5})$ [24]. The complexity of steps (5) and (6) that express the convex problem (30), is $\mathcal{O}(L(N+1)^{3.5})$. As a result, the total complexity of Algorithm 1 is $\mathcal{O}(I_{itr}(M^{3.5} + L(N+1)^{3.5}))$, where I_{itr} represents the iterations number until the convergence criterion is met. This shows that by employing multiple IRSs, computational complexity increases linearly.

4. Simulation results and discussions

In this section, we present the simulation results of evaluating our proposed algorithm and indicate the advantages of using multiple IRSs in improving the secrecy rate of the mmWave networks and also the effect of optimal designing of these surfaces. In our

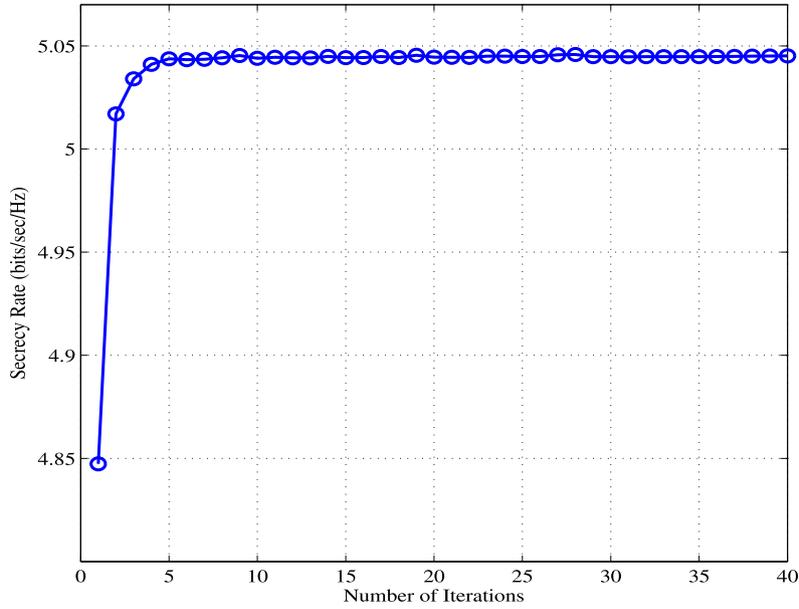


Fig. 2. Convergence of our proposed algorithm.

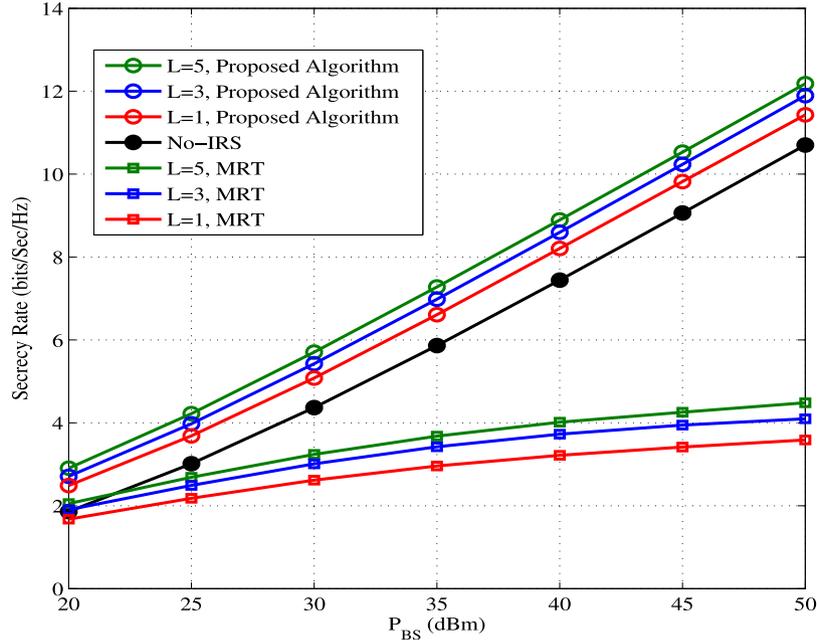


Fig. 3. Secrecy rate versus the BS's transmission power (P_{BS}) for different number of IRSs (with $M = 4$, $N = 16$).

simulations, we assume that a BS with M antennas is located at the center of the polar coordinates. In addition, L IRSs each with N reflecting elements are installed around the BS at the fixed locations to assist in signal transmissions. We assume that the IRSs are located on a circle centered at the BS but with different angle. The L ($L \in \{1, 3, 5\}$) IRSs are placed at $(25 \cos(\frac{\pi}{4} + i\frac{\pi}{12}), 25 \sin(\frac{\pi}{4} + i\frac{\pi}{12}))$ for all $i \in \{-\frac{(L-1)}{2}, -\frac{(L-3)}{2}, \dots, 0, \dots, \frac{(L-3)}{2}, \frac{(L-1)}{2}\}$. Also the user and eavesdropper are located at $(20, \beta)$ and $(18, \beta)$, respectively, where $\beta \sim U[0, \pi/2]$. The noise variances are set as $\sigma_r^2 = \sigma_e^2 = -95$ dBm. $PL(d)$ [dB] is calculated as in (6), (8), (11) and (12), based on $\mu = 72$, $\kappa = 2.92$ and $\sigma_\zeta = 8.7$ and for (9) based on $\mu = 61.4$, $\kappa = 2$ and $\sigma_\zeta = 5.8$ [21].

Maximum Ratio Transmission (MRT) beamforming and No-IRS system are selected as benchmarks for our system performance evaluation. In MRT, conjugate of the channel between the BS and legitimate user is considered as beamforming vector. After

beamforming determination, the reflecting elements phase shifts are obtained using Algorithm 1. Both optimization sub-problems are solved using the CVX optimization toolbox and all the results are averaged over 1000 iterations.

In Fig. 2, the convergence behavior of our proposed algorithm (Algorithm 1) is evaluated. As we discussed in the previous section, the secrecy rate is a non-decreasing function with respect to the number of iterations, thus as it is shown in this figure, by increasing the number of iterations, the secrecy rate also increases and converges to its maximum value after about five iterations.

Fig. 3 shows secrecy rate against BS's transmit power for three different numbers of IRSs ($L = 1, 3, 5$) as well as no-IRS case, where the number of antennas (M) and reflecting elements in each IRS (N) are set to 4 and 16, respectively. It can be seen that an increase in the number of IRSs results in secrecy rate

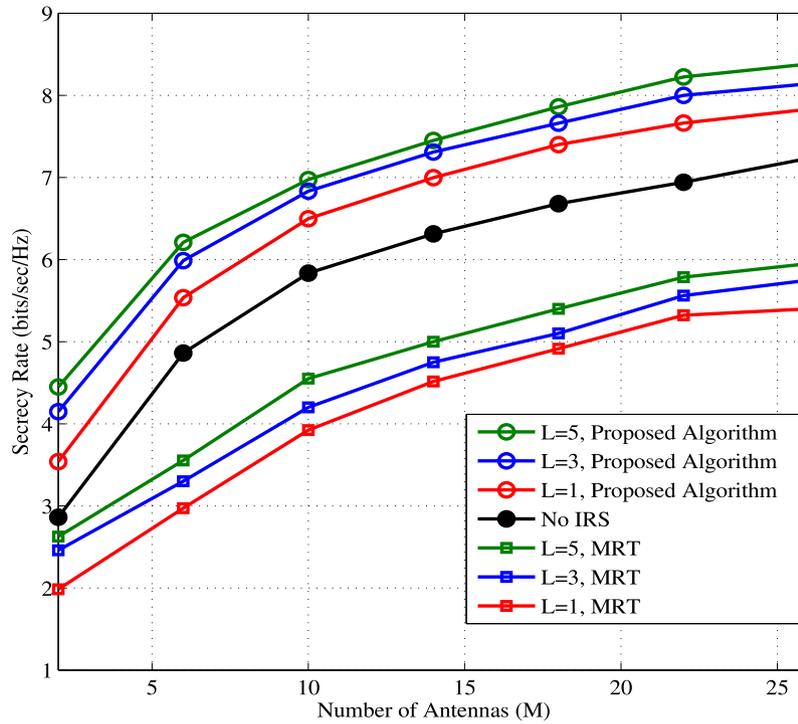


Fig. 4. Secrecy rate versus the number of BS's antennas for different number of IRSs (with $P_{BS} = 35$ dBm).

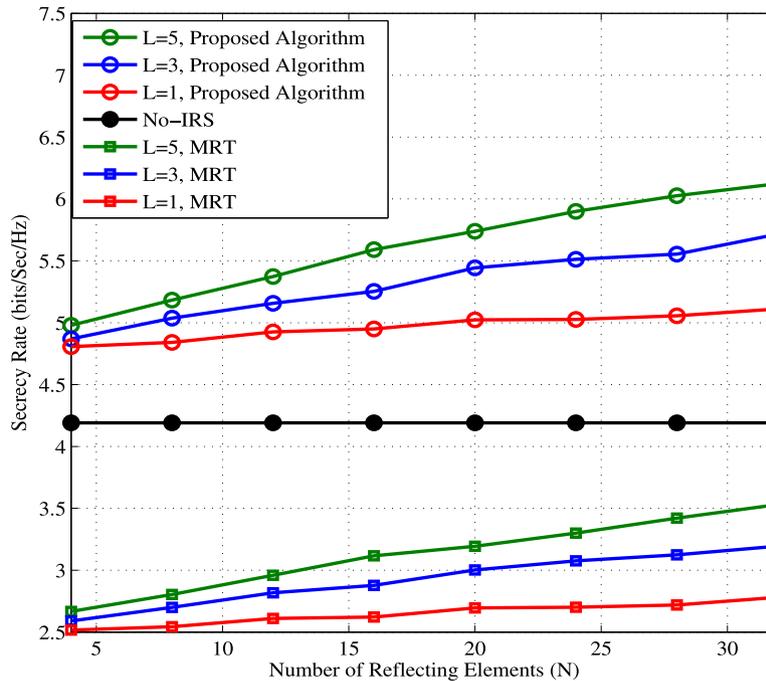


Fig. 5. Secrecy rate versus the number of reflecting elements at each IRS for different number of IRSs.

improvement. This is because a large number of IRSs can lead to strengthening the signal at the user and better user's signal suppression at the eavesdropper. Another interesting point is that the gap between curves decreases by adding more IRSs which means that changing the system from a no-IRS case to the single IRS case has the best system performance improvement and by adding more IRS the value of this improvement is reduced. Since in this paper we tried to consider more practical concerns, we did not ignore the effect of the channel between the BS and

legitimate user and eavesdropper which may have the same probability of existence as the IRS channels. Furthermore, due to BS has multiple antennas and can perform active beamforming, the great significance of the BS beamforming with respect to IRS beamforming can be seen by comparing of the no-IRS curve and MRT related curves. Actually, when MRT is used, the objective to perform active beamforming is not the secrecy rate, and also channel between BS and IRSs are not considered. As a result, the IRS received power is reduced and they do not play

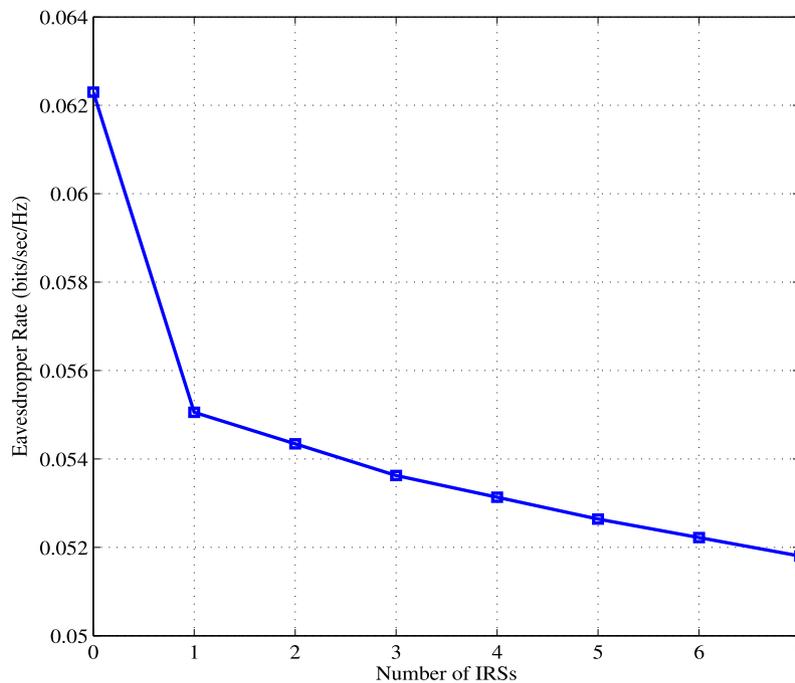


Fig. 6. Eavesdropper rate versus the number of IRSs.

important role in secrecy rate improvement. Therefore, the no-IRS case has better performance than the MRT case with IRS. In contrast to the aforementioned drawbacks of MRT, it has two main advantages. Firstly, this beamforming has lower computational complexity with respect to the optimal beamforming. Secondly, this method can separate IRSs and BS in solving optimization problems which leads to optimization problems that can be handled in a distributed manner.

Fig. 4 illustrates the effect of the number of antennas at the BS on the network secrecy rate for different numbers of IRSs, no-IRS case and also the MRT method. It can be observed due to the more active beamforming gain of BS at a higher number of antennas, the secrecy rate improves by increasing the number of antennas. Similar to the previous figure, the gap between curves by increasing the number of IRSs is reduced. Also due to the earlier mentioned reasons, the MRT method has the least secrecy rate compared with a system with optimal active beamforming.

Fig. 5, shows the secrecy rate versus the number of reflecting elements at the IRSs. As it is expected, with the higher number of IRSs elements, a better secrecy rate is attained. Also, add more reflecting elements introduces more effectiveness of the number of IRSs that is understandable from the gap intensification between the curves. Since in no-IRS case there is no reflecting element, secrecy rate is constant by increasing the number of reflecting elements. Another interesting point is at a higher number of reflecting elements, IRSs play a more important role in system performance and the gap between MRT and the no-IRS case is reduced and this gap among optimal beamforming with IRSs and no-IRS case increases.

Fig. 6 shows the effect of adding more IRSs on eavesdropper rate. As it is shown in this figure and by considering the previous results, we can find that increasing the number of IRSs not only increases the secrecy rate but also decreases the eavesdropper rate. This decrement is reduced at the higher number of IRSs.

5. Conclusions

In this paper, we investigated a multi-IRS mmWave system, where the BS's beamforming vector and the IRSs reflecting elements' phases were jointly optimized to maximize the network

secrecy rate. We solved the resulting non-convex optimization problem using a novel method based on alternating technique and SDR method. Simulation results showed that our proposed method outperforms the case that MRT is used as the beamforming vector at the BS. In addition, we demonstrated that adding more IRSs in the network or increasing the number of elements at each IRS can enhance the performance of the mmWave networks in terms of the secrecy rate.

CRedit authorship contribution statement

Anahid Rafieifar: The main primary idea of this paper, Design, development and analysis in the paper, The simulations are performed, Writing and revision of the paper. **S. Mohammad Razavizadeh:** Design, development and analysis in the paper, Writing and revision of the paper.

Declaration of competing interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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